

# Package: alqrfe (via r-universe)

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**Title** Adaptive Lasso Quantile Regression with Fixed Effects

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**Description** Quantile regression with fixed effects solves longitudinal data, considering the individual intercepts as fixed effects. The parametric set of this type of problem used to be huge. Thus penalized methods such as Lasso are currently applied. Adaptive Lasso presents oracle proprieties, which include Gaussianity and correct model selection. Bayesian information criteria (BIC) estimates the optimal tuning parameter lambda. Plot tools are also available.

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alqrfe-package	<i>Adaptive Lasso Quantile Regression with Fixed Effects</i>
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## Description

Quantile regression with fixed effects solves longitudinal data, considering the individual intercepts as fixed effects. The parametric set of this type of problem used to be huge. Thus penalized methods such as Lasso are currently applied. Adaptive Lasso presents oracle proprieties, which include Gaussianity and correct model selection. Bayesian information criteria (BIC) estimates the optimal tuning parameter lambda. Plot tools are also available.

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**Maintainer**

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**Author(s)**

NA

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 bic\_hat

*Bayesian Information Criteria*


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**Description**

Bayesian Information Criteria

**Usage**

bic\_hat(res, theta, tau, N, p, inf)

**Arguments**

res	Numeric vector, residuals.
theta	Numeric vector, parameters.
tau	Numeric scalar, the percentile.
N	Numeric integer, sample size.
p	Numeric integer, parameter length.
inf	Numeric, internal small quantity.

**Value**

BIC value

---

clean_data	<i>Clean missings</i>
------------	-----------------------

---

**Description**

Clean missings

**Usage**

```
clean_data(y, x, id)
```

**Arguments**

y	Numeric vector, outcome.
x	Numeric matrix, covariates
id	Numeric vector, identifies the unit to which the observation belongs.

**Value**

list with the same objects y, x, id, but without missings.

**Examples**

```
n = 10
m = 4
d = 3
N = n*m
L = N*d
x = matrix(rnorm(L), ncol=d, nrow=N)
subj = rep(1:n, each=m)
alpha = rnorm(n)
beta = rnorm(d)
eps = rnorm(N)
y = x %*% beta + matrix(rep(alpha, each=m) + eps)
```

```

y = as.vector(y)
x[1,3] = NA
clean_data(y=y, x=x, id=subj)

```

---

df_hat	<i>degrees of freedom</i>
--------	---------------------------

---

### Description

This function estimates the degrees of freedom

### Usage

```
df_hat(theta, N, p, inf)
```

### Arguments

theta	Numeric vector, parameters to be test
N	Numeric integer, sample size.
p	Numeric integer, length of theta.
inf	Numeric, internal small quantity.

### Value

degrees of freedom

---

f_den	<i>Kernel density</i>
-------	-----------------------

---

### Description

Kernel density

### Usage

```
f_den(x, inf)
```

### Arguments

x	Numeric vector.
inf	Numeric, internal small quantity.

### Value

y vector, kernel density estimation.

**Examples**

```
x = rnorm(10)
f_den(x, 0.0001)
```

---

f_tab	<i>Tabular function</i>
-------	-------------------------

---

**Description**

Tabular function

**Usage**

```
f_tab(N, n, d, theta, sig2, kind, inf, digt)
```

**Arguments**

N	sample size.
n	length of alpha.
d	length of beta.
theta	Numeric vector.
sig2	Numeric vector.
kind	Numeric, 1 means alpha, 2 means beta
inf	Numeric scalar, internal value, small value.
digt	Numeric integer, round.

---

loss_alqr	<i>Loss adaptive lasso quantile regression with fixed effects</i>
-----------	---

---

**Description**

Loss adaptive lasso quantile regression with fixed effects

**Usage**

```
loss_alqr(theta, x, y, z, tau, n, d, mm, lambda, w)
```

**Arguments**

theta	initial values
x	design matrix
y	vector output
z	incident matrix
tau	percentile
n	N sample size
d	columns of x
mm	n columns of z
lambda	constriction parameter
w	weights

---

`loss_lqr`*Loss lasso quantile regression with fixed effects*

---

**Description**

Loss lasso quantile regression with fixed effects

**Usage**

```
loss_lqr(theta, x, y, z, tau, n, d, mm, lambda)
```

**Arguments**

theta	initial values
x	design matrix
y	vector output
z	incident matrix
tau	percentile
n	N sample size
d	columns of x
mm	n columns of z
lambda	constriction parameter

---

loss_qr	<i>Loss quantile regression</i>
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---

**Description**

Loss quantile regression

**Usage**

loss\_qr(beta, x, y, tau, N, d)

**Arguments**

beta	initial values
x	design matrix
y	vector output
tau	percentile
N	sample size
d	columns of x

---

loss_qrfe	<i>Loss quantile regression with fixed effects</i>
-----------	--

---

**Description**

Loss quantile regression with fixed effects

**Usage**

loss\_qrfe(theta, x, y, z, tau, n, d, mm)

**Arguments**

theta	initial values
x	design matrix
y	vector output
z	incident matrix
tau	percentile
n	N sample size
d	columns of x
mm	n columns of z

---

make_z	<i>Incident matrix Z</i>
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---

**Description**

Create an Incident matrix Z

**Usage**

```
make_z(n, N, id)
```

**Arguments**

n	Numeric integer, number of incidents (subjects, units or individuals).
N	Numeric integer, sample size.
id	Numeric vector of integer, incident identification.

**Value**

Z matrix.

---

mqr	<i>multiple penalized quantile regression</i>
-----	---

---

**Description**

Estimate QR for several taus

**Usage**

```
mqr(x, y, subj, tau = 1:9/10, method = "qr", ngrid = 20, inf = 1e-08, digt = 4)
```

**Arguments**

x	Numeric matrix, covariates
y	Numeric vector, outcome.
subj	Numeric vector, identifies the unit to which the observation belongs.
tau	Numeric vector, identifies the percentiles.
method	Factor, "qr" quantile regression, "qrfe" quantile regression with fixed effects, "lqrfe" Lasso quantile regression with fixed effects, "alqr" adaptive Lasso quantile regression with fixed effects.
ngrid	Numeric scalar greater than one, number of BIC to test.
inf	Numeric scalar, internal value, small value.
digt	Numeric scalar, internal value greater than one, define "zero" coefficient.

**Value**

Beta Numeric array, with three dimensions: 1) tau, 2) coef., lower bound, upper bound, 3) exploratory variables.

**Examples**

```
n = 10
m = 5
d = 4
N = n*m
L = N*d
x = matrix(rnorm(L), ncol=d, nrow=N)
subj = rep(1:n, each=m)
alpha = rnorm(n)
beta = rnorm(d)
eps = rnorm(N)
y = x %*% beta + matrix(rep(alpha, each=m) + eps)
y = as.vector(y)

Beta = mqr(x,y,subj,tau=1:9/10, method="qr", ngrid = 10)
Beta
```

---

mqr\_alpha

*multiple penalized quantile regression - alpha*


---

**Description**

Estimate QR intercepts for several taus

**Usage**

```
mqr_alpha(
  x,
  y,
  subj,
  tau = 1:9/10,
  method = "qr",
  ngrid = 20,
  inf = 1e-08,
  digt = 4
)
```

**Arguments**

x	Numeric matrix, covariates
y	Numeric vector, outcome.
subj	Numeric vector, identifies the unit to which the observation belongs.

tau	Numeric vector, identifies the percentiles.
method	Factor, "qr" quantile regression, "qrfe" quantile regression with fixed effects, "lqrfe" Lasso quantile regression with fixed effects, "alqr" adaptive Lasso quantile regression with fixed effects.
ngrid	Numeric scalar greater than one, number of BIC to test.
inf	Numeric scalar, internal value, small value.
digt	Numeric scalar, internal value greater than one, define "zero" coefficient.

### Value

Alpha Numeric array, with three dimensions: 1) tau, 2) coef., lower bound, upper bound, 3) exploratory variables.

### Examples

```
n = 10
m = 5
d = 4
N = n*m
L = N*d
x = matrix(rnorm(L), ncol=d, nrow=N)
subj = rep(1:n, each=m)
alpha = rnorm(n)
beta = rnorm(d)
eps = rnorm(N)
y = x %*% beta + matrix(rep(alpha, each=m) + eps)
y = as.vector(y)

Alpha = mqr(x,y,subj,tau=1:9/10, method="qr", ngrid = 10)
Alpha
```

---

optim\_alqr

*optim adaptive lasso quantile regression with fixed effects*

---

### Description

This function solves an adaptive lasso quantile regression with fixed effects

### Usage

```
optim_alqr(beta, alpha, wbeta, walpha, x, y, z, tau, N, d, n, ngrid, inf)
```

**Arguments**

beta	Numeric vector, initials values
alpha	Numeric vector, initials values
wbeta	Numeric vector, beta weigths
walpha	Numeric vector, alpha weigths
x	Numeric matrix, covariates.
y	Numeric vector, output.
z	Numeric matrix, incidents.
tau	Numeric scalar, the percentile.
N	Numeric integer, sample size.
d	Numeric integer, X number of columns.
n	Numeric integer, length of alpha.
ngrid	Numeric integer, number of interactions of BIC.
inf	Numeric, internal small quantity.

**Value**

parametric vector and residuals

---

optim_lqr	<i>optim lasso quantile regression with fixed effects</i>
-----------	---

---

**Description**

This function solves a lasso quantile regression with fixed effects

**Usage**

```
optim_lqr(beta, alpha, x, y, z, tau, N, d, n, ngrid, inf)
```

**Arguments**

beta	Numeric vector, initials values
alpha	Numeric vector, initials values
x	Numeric matrix, covariates.
y	Numeric vector, output.
z	Numeric matrix, incidents.
tau	Numeric scalar, the percentile.
N	Numeric integer, sample size.
d	Numeric integer, X number of columns.
n	Numeric integer, length of alpha.
ngrid	Numeric integer, number of interactions of BIC.
inf	Numeric, internal small quantity.

**Value**

parametric vector and residuals

---

optim_qr	<i>optim quantile regression</i>
----------	----------------------------------

---

**Description**

This function solves a quantile regression

**Usage**

```
optim_qr(beta, x, y, tau, N, d)
```

**Arguments**

beta	Numeric vector, initials values.
x	Numeric matrix, covariates.
y	Numeric vector, output.
tau	Numeric scalar, the percentile.
N	Numeric integer, sample size.
d	Numeric integer, X number of columns.

**Value**

parametric vector and residuals.

---

optim_qrfe	<i>optim quantile regression with fixed effects</i>
------------	---

---

**Description**

This function solves a quantile regression with fixed effects

**Usage**

```
optim_qrfe(beta, alpha, x, y, z, tau, N, d, n)
```

**Arguments**

beta	Numeric vector, initials values
alpha	Numeric vector, initials values
x	Numeric matrix, covariates.
y	Numeric vector, output.
z	Numeric matrix, incidents.
tau	Numeric scalar, the percentile.
N	Numeric integer, sample size.
d	Numeric integer, X number of columns.
n	Numeric integer, length of alpha.

**Value**

parametric vector and residuals

---

plot_alpha	<i>plot multiple penalized quantile regression - alpha</i>
------------	--

---

**Description**

plot QR intercepts for several taus

**Usage**

```
plot_alpha(
  Beta,
  tau = 1:9/10,
  D,
  ylab = expression(alpha[1]),
  col = 2,
  lwd = 1,
  lty = 2,
  pch = 1,
  cex.axis = 1,
  cex.lab = 1,
  main = ""
)
```

**Arguments**

Beta	Numeric array, with three dimensions: 1) tau, 2) coef., lower bound, upper bound, 3) exploratory variables.
tau	Numeric vector, identifies the percentiles.
D	intercept's number.

ylab	y legend
col	color.
lwd	line width.
lty	line type.
pch	point character.
cex.axis	cex axis length.
cex.lab	cex axis length.
main	title.

### Examples

```

n = 10
m = 5
d = 4
N = n*m
L = N*d
x = matrix(rnorm(L), ncol=d, nrow=N)
subj = rep(1:n, each=m)
alpha = rnorm(n)
beta = rnorm(d)
eps = rnorm(N)
y = x %*% beta + matrix(rep(alpha, each=m) + eps)
y = as.vector(y)

Beta = mqr_alpha(x,y,subj,tau=1:9/10, method="qr", ngrid = 10)
plot_alpha(Beta,tau=1:9/10,D=1)

```

---

plot\_taus

*plot multiple penalized quantile regression*

---

### Description

plot QR for several taus

### Usage

```

plot_taus(
  Beta,
  tau = 1:9/10,
  D,
  col = 2,
  lwd = 1,
  lty = 2,
  pch = 1,
  cex.axis = 1,
  cex.lab = 1,
  main = ""
)

```

**Arguments**

Beta	Numeric array, with three dimensions: 1) tau, 2) coef., lower bound, upper bound, 3) exploratory variables.
tau	Numeric vector, identifies the percentiles.
D	covariate's number.
col	color.
lwd	line width.
lty	line type.
pch	point character.
cex.axis	cex axis length.
cex.lab	cex axis length.
main	title.

**Examples**

```

n = 10
m = 5
d = 4
N = n*m
L = N*d
x = matrix(rnorm(L), ncol=d, nrow=N)
subj = rep(1:n, each=m)
alpha = rnorm(n)
beta = rnorm(d)
eps = rnorm(N)
y = x %*% beta + matrix(rep(alpha, each=m) + eps)
y = as.vector(y)

Beta = mqr(x,y,subj,tau=1:9/10, method="qr", ngrid = 10)
plot_taus(Beta,tau=1:9/10,D=1)

```

---

```
print.ALQRFE
```

```
Print an ALQRFE
```

---

**Description**

Define the visible part of the object class ALQRFE

**Usage**

```
## S3 method for class 'ALQRFE'
print(x, ...)
```

**Arguments**

x	An object of class "ALQRFE"
...	further arguments passed to or from other methods.

---

qr	<i>quantile regression</i>
----	----------------------------

---

**Description**

Estimate quantile regression with fixed effects for one tau

**Usage**

```
qr(x, y, subj, tau = 0.5, method = "qr", ngrid = 20, inf = 1e-08, digt = 4)
```

**Arguments**

x	Numeric matrix, covariates
y	Numeric vector, outcome.
subj	Numeric vector, identifies the unit to which the observation belongs.
tau	Numeric, identifies the percentile.
method	Factor, "qr" quantile regression, "qrfe" quantile regression with fixed effects, "lqrfe" Lasso quantile regression with fixed effects, "alqr" adaptive Lasso quantile regression with fixed effects.
ngrid	Numeric scalar greater than one, number of BIC to test.
inf	Numeric scalar, internal value, small value.
digt	Numeric scalar, internal value greater than one, define "zero" coefficient.

**Value**

alpha Numeric vector, intercepts' coefficients.  
beta Numeric vector, exploratory variables' coefficients.  
lambda Numeric, estimated lambda.  
res Numeric vector, percentile residuals.  
tau Numeric scalar, the percentile.  
penalty Numeric scalar, indicate the chosen effect.  
sig2\_alpha Numeric vector, intercepts' standard errors.  
sig2\_beta Numeric vector, exploratory variables' standard errors.  
Tab\_alpha Data.frame, intercepts' summary.  
Tab\_beta Data.frame, exploratory variables' summary.  
Mat\_alpha Numeric matrix, intercepts' summary.  
Mat\_beta Numeric matrix, exploratory variables' summary.  
method Factor, method applied.

## References

Koenker, R. (2004) "Quantile regression for longitudinal data", *J. Multivar. Anal.*, 91(1): 74-89, <doi:10.1016/j.jmva.2004.05.006>

## Examples

```
# Example 1
n = 10
m = 5
d = 4
N = n*m
L = N*d
x = matrix(rnorm(L), ncol=d, nrow=N)
subj = rep(1:n, each=m)
alpha = rnorm(n)
beta = rnorm(d)
eps = rnorm(N)
y = x %*% beta + matrix(rep(alpha, each=m) + eps)
y = as.vector(y)
m1 = qr(x,y,subj,tau=0.75, method="qrfe")
m1
m2 = qr(x,y,subj,tau=0.3, method="lqrfe", ngrid = 10)
m2

# Example 2, from MASS package
Rabbit = MASS::Rabbit
Rabbit$Treatment = ifelse(Rabbit$Treatment=="Control",0,1)
Rabbit$Animal = ifelse(Rabbit$Animal == "R1",1,ifelse(Rabbit$Animal == "R2",2,
ifelse(Rabbit$Animal == "R3",3,ifelse(Rabbit$Animal == "R4",4,5))))
X = matrix(cbind(Rabbit$Dose,Rabbit$Treatment), ncol=2)
m3 = qr(x=X, y=Rabbit$BPchange, subj=Rabbit$Animal,tau=0.5, method="alqrfe", ngrid = 10)
m3
```

---

q\_cov

*Covariance*

---

## Description

Estimate Covariance matrix

## Usage

```
q_cov(alpha, beta, d, inf, n, N, res, method, tau, X, Z)
```

## Arguments

alpha	Numeric vector.
beta	Numeric vector.

d	length of beta.
inf	Numeric scalar, internal value, small value.
n	length of alpha.
N	sample size.
res	Numeric vector, residuals.
method	Factor, "qr" quantile regression, "qrfe" quantile regression with fixed effects, "lqrfe" Lasso quantile regression with fixed effects, "alqr" adaptive Lasso quantile regression with fixed effects.
tau	Numeric, identifies the percentile.
X	Numeric matrix, covariates.
Z	Numeric matrix, incident matrix.

---

rho_koenker	<i>Rho Koenker</i>
-------------	--------------------

---

**Description**

Rho Koenker

**Usage**

rho\_koenker(x, tau)

**Arguments**

x	generic vector
tau	percentile

---

sgf	<i>Identify significance</i>
-----	------------------------------

---

**Description**

Identify significance

**Usage**

sgf(x)

**Arguments**

x	Numeric vector.
---	-----------------

**Value**

y vector Factor, symbol flag of significant p-values.

**Examples**

```
n = 10  
pvalue = rgamma(10,1,10)  
sgf(pvalue)
```

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